

TEOREMA 17 - Se f è CONT. IN I , DERIV. IN $\overset{\circ}{I}$,

5.24

$$f \text{ STRETT. CRESC. IN UN INTERVALLO } I \iff \begin{cases} \text{j) } \forall x \in \overset{\circ}{I}, f'(x) \geq 0 \\ \text{jj) } \nexists J \subset I: \forall x \in J, f'(x) = 0 \end{cases}$$

DIM.

" \Rightarrow "

$$\approx \text{j)} \approx \text{p.a. } \exists x_0 \in \overset{\circ}{I}: f'(x_0) < 0 \Rightarrow f \text{ STRETT. DECR. IN } x_0$$

$$\approx \text{jj)} \approx \text{p.a. } \exists J \subset I: \forall x \in J, f'(x) = 0 \Rightarrow f(x) = \text{cost.}, \forall x \in J$$

" \Leftarrow "

$$\text{j)} \Rightarrow f \text{ CRESC. IN } I \iff [\forall x', x'' \in I: x' < x'' \Rightarrow f(x') \leq f(x'')]$$

$$\text{p.a. } f(x') = f(x'')$$

$$\left. \begin{array}{l} \forall x \in [x', x''], \quad x' < x \Rightarrow f(x') \leq f(x) \\ \quad \quad \quad x < x'' \Rightarrow f(x) \leq f(x'') \end{array} \right\} \Rightarrow$$

$$\Rightarrow \forall x \in [x', x''], \quad f(x') = f(x) = f(x'')$$

$$\Rightarrow \forall x \in [x', x''], \quad f'(x) = 0$$

□